



January, 2002

## Collection of Magnetics Equations

### Notations

V= Voltage [Volts]

I = Current [Amp]

$\phi$ = Magnetic flux [Weber]

B= Flux density [Tesla, ;  $\frac{\text{Weber}}{\text{m}^2}$ ; 10,000 Gauss]

L= Inductance [Henry]

$A_e$  = Core effective area [m]

$l_e$ = Core effective length

$\mu$  = Magnetic permeability [ $\frac{\text{Amperes}}{\text{m}}$ ]

$\mu_r$ =Relative permeability

$\mu_0$ = Permeability constant [ $1.26 \cdot 10^{-6} \frac{\text{Henry}}{\text{m}}$ ]

$\mu_e$ = Effective permeability constant [ $1.26 \cdot 10^{-6} \frac{\text{Henry}}{\text{m}}$ ]

$L_g$  = Effective air gap length [m]

$l_c$  = Core length (less gap) [m]

$l_e$ = Effective core length [m]

H = Magnetic field [ $\frac{\text{Amperes}}{\text{m}}$ ]

$H_c$ = Magnetic field in core [ $\frac{\text{Amperes}}{\text{m}}$ ]

$H_g$ = Magnetic field in gap [ $\frac{\text{Amperes}}{\text{m}}$ ]

$A_w$  = winding window area [m<sup>2</sup>]

J = Current density [ $\frac{\text{Amperes}}{\text{m}^2}$ ]

$I_{rms}$  = effective current [Amperes]

$I_{pk}$ = Peak current [Amperes]

n = Number of turns

$T_s$  = Switching period [Seconds]

$f_s$ = Switching frequency [ $\frac{1}{\text{Seconds}}$ ]

$P_p$  = Primary power [Watts]

$P_s$ = Secondary power [Watts]

K = Packing coefficient

S = Skin depth [mm]



## 1. Inductor

### 1.1 Basic Equations

$$V = L \frac{dI}{dt} \quad (1)$$

$$V = n \frac{d\phi}{dt} \quad (2) \quad ; \quad \phi = B A_e$$

$$\implies 1 = \frac{L}{n} \frac{dI}{d\phi} \implies n A_e \int dB = L \int dI \implies n A_e B_{max} = L I_{pk}$$

$$n = \frac{L I_{pk}}{A B_{max}} \quad (3) \implies A_e = \frac{L I_{pk}}{n B_{max}} \quad (4)$$

$$n I_{rms} = J A_w K \quad (5) \implies n = \frac{A_w J k}{I_{rms}} \quad (6)$$

$$A_e A_w = A_p = \frac{L I_{pk} I_{rms}}{J K B_{max}} \quad (7)$$

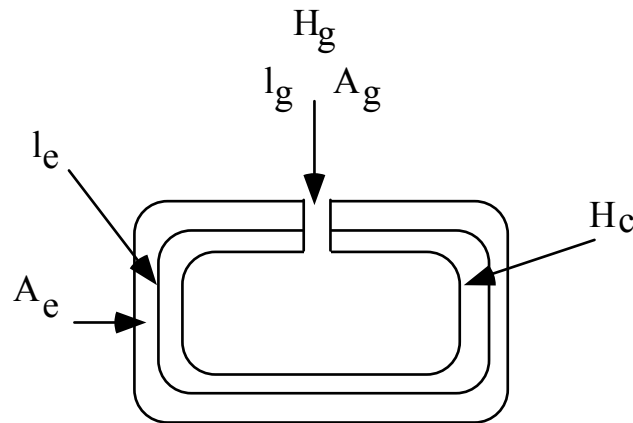
$$B = \mu H = \frac{\mu n I}{l_e} \quad (8); \quad B_{max} = \frac{\mu n I_{pk}}{l_e} \implies n = \frac{B_{max} l_e}{\mu I_{pk}} \quad (9)$$

$$A_e = \frac{L I_{pk}}{n B_{max}} \implies A_e = \frac{L I_{pk}}{\frac{B_{max} l_e}{\mu I_{pk}} B_{max}} \quad (10)$$

$$A_e l_e = \text{Volume (core)} = \frac{L I_{pk}^2 \mu}{B_{max}^2} \quad (11)$$



## 1.2 Air Gapped Inductor



$$B = \mu_e \frac{nI}{l_e} \quad (12)$$

$$nI = H_g l_g + H_c l_c = \frac{B_g}{\mu_g} l_g + \frac{B_c}{\mu_c} l_c \quad (13)$$

$$B = B_g = B_c \implies nI = B \left( \frac{l_g}{\mu_g} + \frac{l_c}{\mu_c} \right) \implies B = \frac{nI}{\frac{l_g}{\mu_g} + \frac{l_c}{\mu_c}} \quad (14)$$

$$B = \mu_e \frac{nI}{l_e} = \frac{nI}{\frac{l_g}{\mu_g} + \frac{l_c}{\mu_c}} \implies \mu_e = \frac{l_e}{\frac{l_g}{\mu_g} + \frac{l_c}{\mu_c}} \quad (15)$$

Assuming:

$$\mu_g \ll \mu_c ; \quad \frac{l_c}{\mu_c} < \frac{l_g}{\mu_g} ; \quad l_e = l_g + l_c ; \quad l_c ; \quad \mu_g = \mu_0 \quad (16)$$

$$\mu_e = \mu_g \frac{l_e}{l_g} \implies \mu_0 \frac{l_e}{l_g} \implies \mu_r \frac{l_c}{l_g} \quad (17)$$



## 2. Square -Wave Transformer

$$V = n A_e \frac{dB}{dt} \implies \int V dt = n A_e \Delta B \implies \frac{V}{2 f_s} = n A_e \Delta B \quad (18)$$

$$n I_{rms} = A_w J k \implies n = \frac{A_w J K}{I_{rms}} \quad (19)$$

$$\frac{V}{2 f_s} = \frac{A_w J K}{I_{rms}} \Delta B \quad (20)$$

$$A_e A_w = A_p = \frac{V I_{rms}}{2 f_s J K \Delta B}$$

$$A_p = \frac{P_p + P_s}{2 f_s J K \Delta B} = \frac{T_s (P_p + P_s)}{2 f_s J K \Delta B} \quad (21)$$

## 3. Skin Depth

$$S = \frac{72}{\sqrt{f_s}} \quad (22)$$