

Cooperation in Multiple Access Channels with States

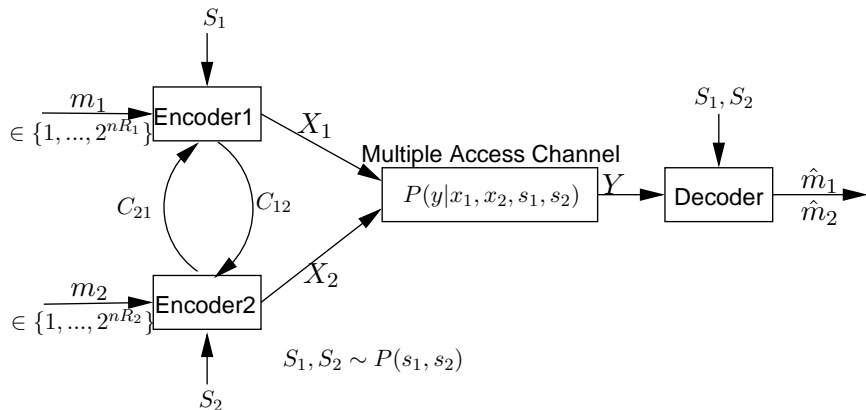
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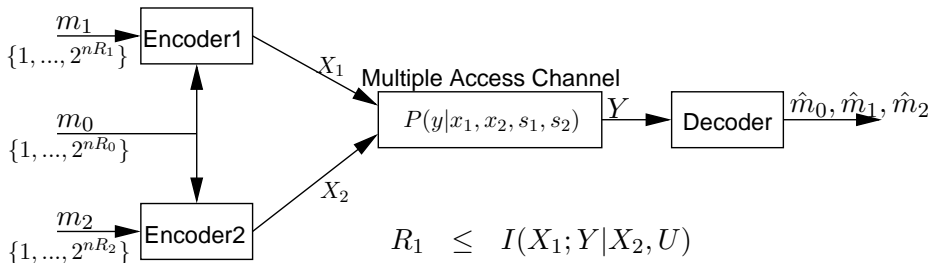
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The communication setting considered in the talk



- Encoders have different partial state information
- This setting captures the idea of, simultaneously, sharing a part of the private messages m_1, m_2 and sharing the information on channel state (S_1, S_2) .

Background : Memoryless MAC (Multiple Access Channel) with common message



$$R_1 \leq I(X_1; Y | X_2, U)$$

$$R_2 \leq I(X_2; Y | X_1, U)$$

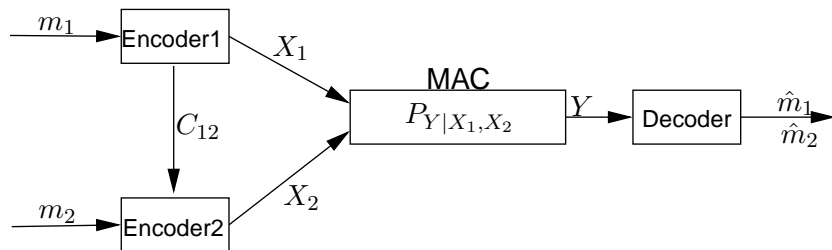
$$R_1 + R_2 \leq I(X_1, X_2; Y | U)$$

$$R_0 + R_1 + R_2 \leq I(X_1, X_2; Y)$$

for $P(u)P(x_1|u)P(x_2|u)P(y|x_1, x_2)$.

[Slepian/Wolf73]

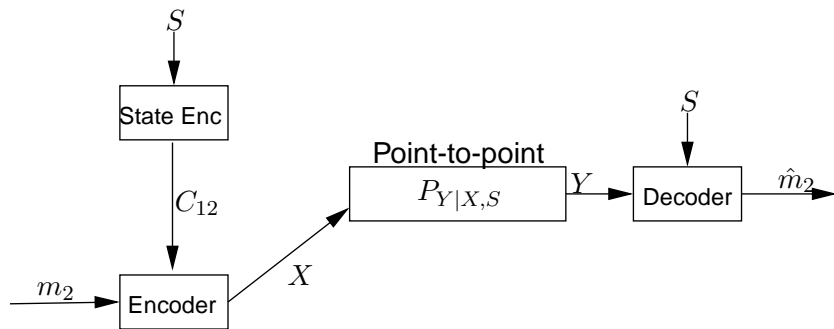
Memoryless MAC - Message cooperation



- Optimal coding scheme: Encoder 2 obtains part of the private message m_1 and use it as common message scheme m'_0 . $R'_0 = C_{12}$, $R'_1 = R_1 - C_{12}$, $R'_2 = R_2$.

[Willems82]

Special case: Point-to-point with encoded state information



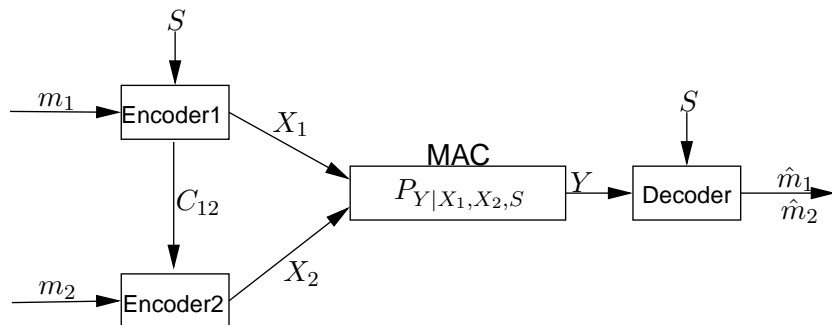
$$C_{12} \geq I(U; S),$$

$$R \leq I(X; Y, S|U) = I(X; Y|S, U),$$

for $P(s)P(u|s)P(x|u)P(y|x, s)$.

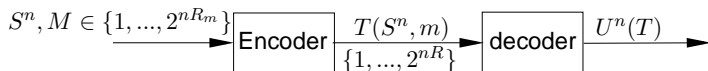
[Cemal/Steinberg07]

Message-state cooperation



- Encoder 1 and Decoder have state information
- This setting captures the idea of, simultaneously, sharing a part of the private message m_1 and sharing the information on channel state S .

Simplified problem



S^n is i.i.d., $S \sim P(s)$

Generate a sequence U^n such that

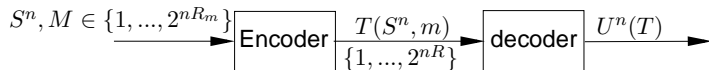
- 1 U^n is jointly typical with S^n , i.e.,

$$\lim_{n \rightarrow \infty} \Pr\{(U^n, S^n) \in T_\epsilon^{(n)}(U, S)\} = 1,$$

- 2 there exists a function $g(U^n)$ such that

$$\lim_{n \rightarrow \infty} \Pr\{g(U^n) \neq M\} = 0.$$

Simplified problem-solution



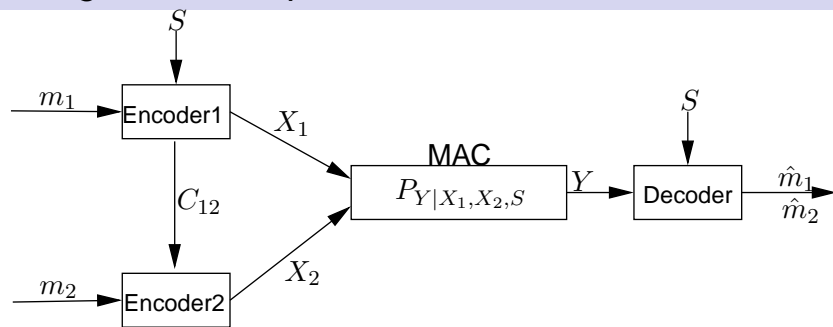
S^n is i.i.d., $S \sim P(s)$

Theorem

$R > R_m + I(U; S)$ and $H(U|S) \geq R_m$.

- 1 Generate 2^{nR_m} bins, in each bin $2^{n(I(U;S)+\epsilon)}$ codewords, generated i.i.d. $\sim P(u)$.
- 2 The message is associated with Bin.
- 3 A codeword is chosen from the bin to be jointly typical with S^n .

Message-state cooperation



Theorem

$$C_{12} \geq I(U; S)$$

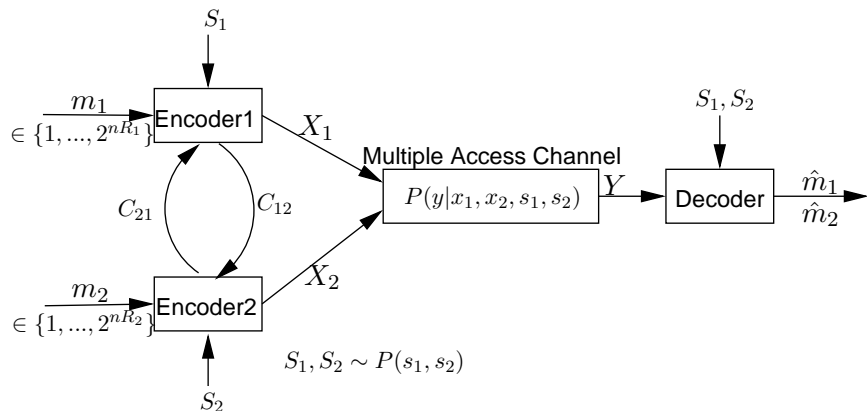
$$R_1 \leq I(X_1; Y | X_2, S, U) + C_{12} - I(U; S)$$

$$R_2 \leq I(X_2; Y | X_1, S, U)$$

$$R_1 + R_2 \leq \min \left\{ \begin{array}{l} I(X_1, X_2; Y | S, U) + C_{12} - I(U; S), \\ I(X_1, X_2; Y | S) \end{array} \right\},$$

for distributions $P(s)P(u, x_1|s)P(x_2|u)P(y|x_1, x_2, s)$.

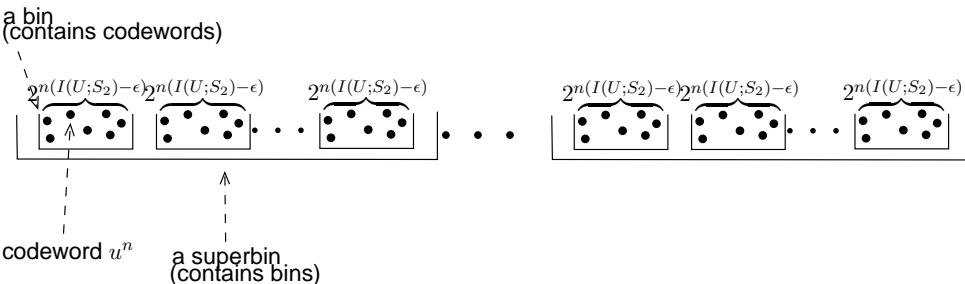
General case



Here a double binning is needed.

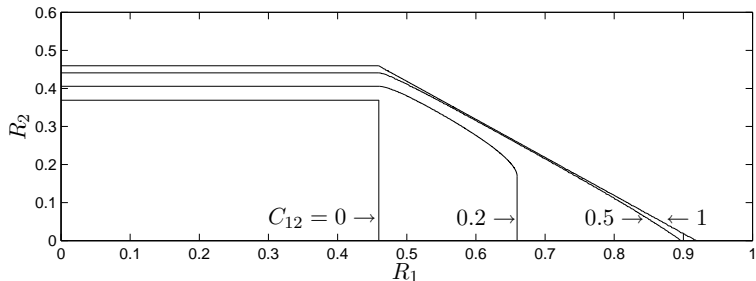
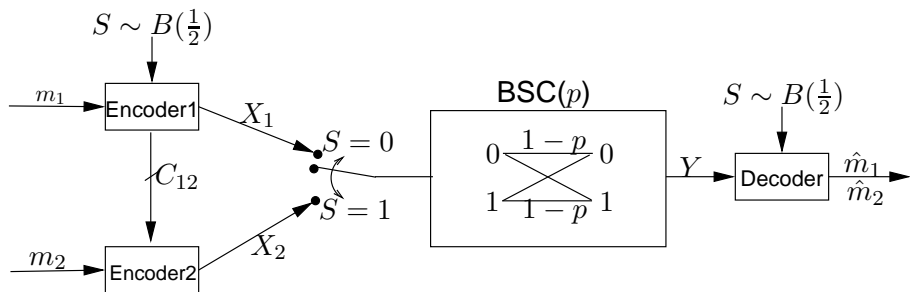
- 1 First layer for generating coordination, as in Wyner-Ziv.
- 2 Second layer for transmitting a message.

Combining message and state using new double binning

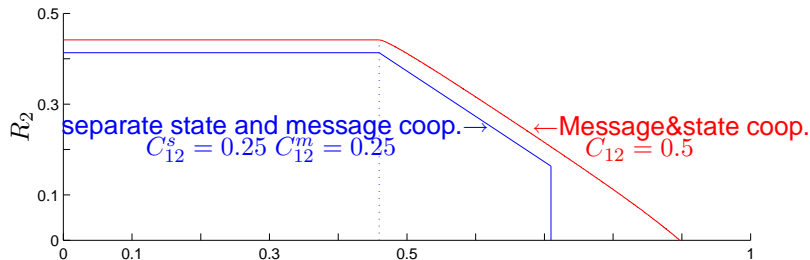
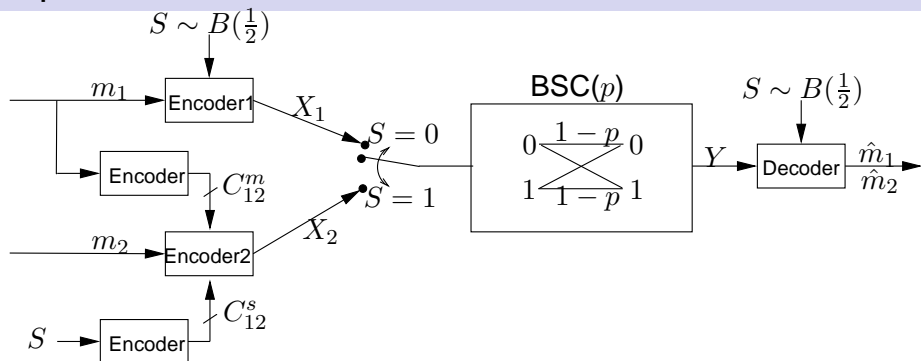


- consists of two-layer bins (codes), where in the first layer we have bins(codes) that contain codewords and in the second layer we have superbins that contain bins.

Example



Separate links for state and for coordination



Summary

- We investigated MAC with cooperating encoders and partial state information.
- The cooperation has a two-fold purpose:
 - generating empirical state coordination
 - sharing the private messages
- Double binning- an optimal technique for combining state and message
- Message and state cooperation strictly increases the capacity.

Summary

- We investigated MAC with cooperating encoders and partial state information.
- The cooperation has a two-fold purpose:
 - generating empirical state coordination
 - sharing the private messages
- Double binning- an optimal technique for combining state and message
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Thank you very much !